## CENTRAL LIBRARY N.C.COLLEGE

# 2022/TDC(CBCS)/EVEN/SEM/ ECOHCC-202T/502

TDC (CBCS) Even Semester Exam., 2022

**ECONOMICS** 

(Honours)

(2nd Semester)

Course No.: ECOHCC-202T

( Mathematical Methods in Economics—II )

Full Marks: 70
Pass Marks: 28

Time: 3 hours

The figures in the margin indicate full marks for the questions

### SECTION—A

Answer any ten questions:

 $2 \times 10 = 20$ 

- 1. Define first-order linear differential equations.
- 2. Solve

$$\frac{dy}{dx} + 2x = 0$$

with initial condition y(0) = 5.

(Turn Over)

(3)

- 3. Define an exact differential equation.
- 4. Write two differences between scalar product and vector product.
- 5. What is orthogonal matrix? Give one example.
- 6. What is total differential?
- 7. Mention two characteristics of homogeneous function.
- 8. Given

$$y = 3x_1 + \frac{x_1}{x_2} + 10x_2^2$$

Find  $\frac{\partial y}{\partial x_1}$ .

- 9. Mention two characteristics of convex function.
- 10. Mention the geometric definition of concavity and convexity for a two-variable function  $z = f(x_1, x_2)$ .
- 11. What is unconstrained optimization?
- 12. What is technology coefficient matrix?

13. Write the economic meaning of

$$\sum_{i=1}^n a_{ij} < 1$$

in Leontief static open model.

- 14. Write two assumptions of technology coefficient matrix (A) in Leontief static open model.
- 15. Mention two limitations of Leontief static open input-output model.

#### SECTION-B

Answer any five questions:

10×5=50

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16. (a) Find the solution of the following differential equation:

$$\frac{dy}{dx} + 3x^2y = 3x^2$$

b) Solve:

$$3\frac{dy}{dt} + 6y = 5$$
;  $y(0) = 0$ 

(c) Write down the general procedure of solving exact differential equation.

(4)

17. (a) Given

$$Q_d = 10 - 5P$$

$$Q_s = -10 + 5P$$

$$\frac{dp}{dr} = 3(Q_d - Q_s)$$

Analyze the market model for stability. 4

- (b) Distinguish between homogeneous and non-homogeneous equations.
- (c) Write the method of solution of second-order linear differential equation.

18. (a) Given

$$|A| = \begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix}$$

Show that |A| = |A'|.

(b) If

$$\begin{vmatrix} k-2 & 1 \\ 5 & k+2 \end{vmatrix} = 0$$

then find k.

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(c) Solve the following system of simultaneous equations by matrix inversion:

$$2x_1 + 3x_2 - x_3 = 15$$
$$4x_2 + 2x_3 = 16$$
$$3x_1 + 2x_2 = 18$$

19. (a) Solve the linear market model:

$$Q_d = 50 - 2P$$

$$Q_s = -10 + 3P$$

$$Q_d = Q_s$$

(b) In a two-economy model denoted by the subscripts 1 and 2

$$C_1 = 0.8Y_1$$

$$M_1 = 0.2Y_1$$

$$Y_1 = C_1 + 200 + (X_1 - M_1)$$

$$X_1 = M_2$$

$$C_2 = 0.7Y_2$$

$$C_2 = 0.7Y_2$$

$$M_2 = 0.15Y_2$$

$$Y_2 = C_2 + 100 + (X_2 - M_2)$$

$$X_2 = M_1$$

find the equilibrium national incomes  $Y_1$  and  $Y_2$  using matrix algebra.

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Given (a) 20.

$$y = 10 + 2x_1^2x_2 + 3x_2^2x_3^2$$

second-order Find partial derivatives.

Given (b)

$$y = x_1^2 + 2x_2$$
 where  $x_2 = x_1^3 + 5$ 

Find out total derivative  $\frac{dy}{dx_1}$ .

If the utility function is

$$u = \log(ax_1 + bx_2 + c\sqrt{x_1x_2})$$

obtain the ratio of marginal utility.

Given a demand function in implicit 21. form

$$F(Q_1, P_1, P_2, Y) = 10P_1Q_1 + 5Q_1 - 2P_2 - 4Y - 18 = 0$$

Use implicit function rule to find-

- (i) own price elasticity,  $E_{11}$ ;
- (ii) cross-price elasticity,  $E_{12}$ ;
- (iii) income elasticity at a point  $(P_1, P_2, Y) = (2, 1, 20).$

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- Given the function  $Q = AK^{\alpha}L^{\beta}$ , where  $A, \alpha, \beta$  are parameters and positive.
  - (i) Show that the function is a linear homogeneous function.
  - (ii) Prove that

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$$K\frac{\partial Q}{\partial K} + L\frac{\partial Q}{\partial L} = Q$$

when the function is linearly homogeneous.

- Mention the characteristics of convex function with more than one explanatory variable.
  - Derive the first- and second-order conditions in order to show that indifference curve is negatively sloped and convex to the origin taking the utility function u = f(x, y), where u = total utility, x and y are the quantities of two commodities.
- 23. (a) Find the extreme values of the function

$$y = 4x_1^3 + 8x_1x_2 - 4x_1^2 - x_2^2 + 10$$

Given the utility function u = 2xusubject to the budget constraint 3x + 4y = 90. Find out the equilibrium values of x and y that maximize total utility.

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- 24. Derive the conditions for viability of output in Leontief static open input-output model.
- 25. Given the technology coefficient matrix

$$A = \begin{bmatrix} 0 \cdot 2 & 0 \cdot 4 \\ 0 \cdot 3 & 0 \cdot 1 \end{bmatrix}$$

Labour requirement to produce single unit of output in each industry respectively 0.3 and 0.2 and final demand

$$C = \begin{bmatrix} 40 \\ 50 \end{bmatrix}$$

- (a) Find out equilibrium levels of output in each industry.
- (b) Find out total labour requirements in both the industries.
- (c) Obtain gross value added in both the industries.



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